

ADT Graf

- **ADT Graph** er i JDSL en **positional container** hvor posisjonene er noder og kanter i grafen.

- Metoder arvet fra **Positional Container**:

- `size()` Antall kanter pluss noder.
- `isEmpty()`
- `elements()`
- `positions()`
- `swap()`
- `replaceElement()`

Notasjon: Graph G ; Vertices v, w ; Edge e ; Object o

- Metoder arvet fra **InspectableGraph**

- `numVertices()`
Return the number of vertices of G .
- `numEdges()`
Return the number of edges of G .
- `vertices()`
Return an enumeration of the vertices of G .
- `edges()`
Return enumeration of the edges of G .

1

Fra InspectableGraph

- `directedEdges()`
Return an enumeration of all directed edges in G .
- `undirectedEdges()`
Return an enumeration of all undirected edges in G .
- `incidentEdges(v)`
Return an enumeration of all edges incident on v .
- `inIncidentEdges(v)`
Return an enumeration of all the incoming edges to v .
- `outIncidentEdges(v)`
Return an enumeration of all the outgoing edges from v .
- `opposite(v, e)`
Return an endpoint of e distinct from v .
- `degree(v)`
Return the degree of v .
- `inDegree(v)`
Return the in-degree of v .
- `outDegree(v)`
Return the out-degree of v .

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Fra InspectableGraph

- `adjacentVertices(v)`
Return an enumeration of the vertices adjacent to v .
- `inAdjacentVertices(v)`
Return an enumeration of the vertices adjacent to v along incoming edges.
- `outAdjacentVertices(v)`
Return an enumeration of the vertices adjacent to v along outgoing edges.
- `areAdjacent(v, w)`
Return whether vertices v and w are adjacent.
- `endVertices(e)`
Return an array of size 2 storing the end vertices of e .
- `origin(e)`
Return the end vertex from which e leaves.
- `destination(e)`
Return the end vertex at which e arrives.
- `isDirected(e)`
Return true iff e is directed.

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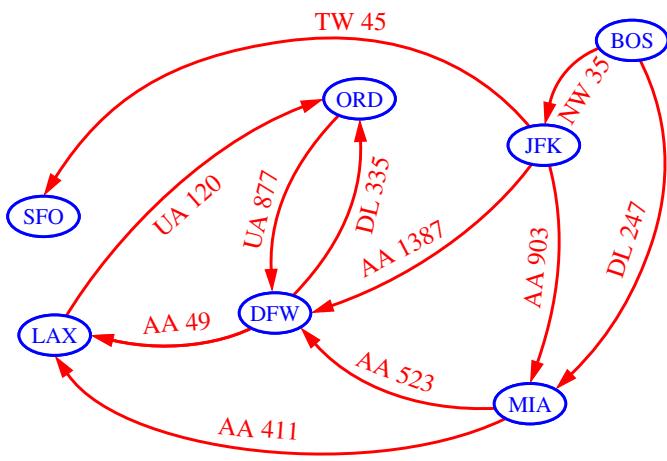
Oppdateringsmetoder i Graph:

- `makeUndirected(e)`
Set e to be an undirected edge.
- `reverseDirection(e)`
Switch the origin and destination vertices of e .
- `setDirectionFrom(e, v)`
Sets the direction of e away from v .
- `setDirectionTo(e, v)`
Sets the direction of e toward v , one of its end vertices.
- `insertEdge(v, w, o)`
Insert and return an undirected edge between v and w , storing o at this position.
- `insertDirectedEdge(v, w, o)`
Insert and return a directed edge between v and w , storing o at this position.
- `insertVertex(o)`
Insert and return a new (isolated) vertex storing o at this position.
- `removeEdge(e)`
Remove edge e .

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Implementasjon av ADT Graph

- Hvordan representere en graf?
- Vi lagrer **noder** og **kanter** i to containere, og hver kant peker til nodene den knytter sammen.

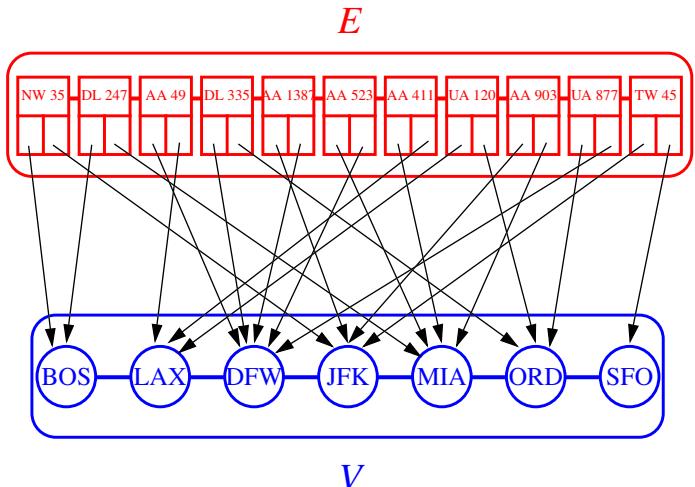


- I tillegg: 1)Kantliste, 2)Naboliste, 3)Nabomatrise

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Kantliste

- Kantliste**-strukturen lagrer noder og kanter som usorterte sekvenser.
- Lett å implementere.
- Det å finne alle kanter tilhørende en node tar lang tid: må gå gjennom alle kanter.



V

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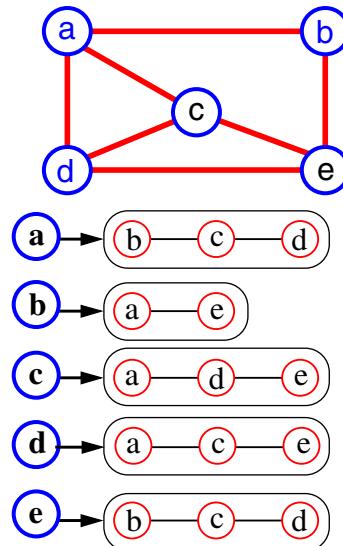
Kjøretid for Kantliste-operasjoner

Operasjon	Tid
size, isEmpty, replaceElement, swap	O(1)
numVertices, numEdges	O(1)
vertices	O(n)
edges, directedEdges, undirectedEdges	O(m)
elements, positions	O(n+m)
endVertices, opposite, origin, destination, isDirected	O(1)
incidentEdges, inIncidentEdges, outIncidentEdges, adjacentVertices, inAdjacentVertices, outAdjacentVertices, areAdjacent, degree, inDegree, outDegree	O(m)
insertVertex, insertEdge, insertDirectedEdge, removeEdge, makeUndirected, reverseDirection, setDirectionFrom, setDirectionTo	O(1)
removeVertex	O(m)

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NaboListe (uten egne kantobjekter)

- naboliste for en node v:**
sekvens av noder som er nabo til **v**
- representer grafen ved egen nabolist for hver noder

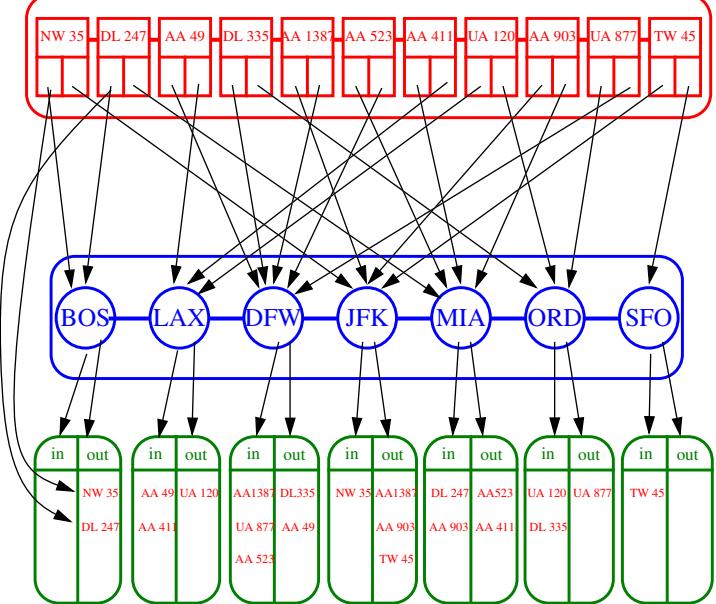


$$\text{Minnebruk} = O(N + \sum_{v \in V} \deg(v)) = O(N + M)$$

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NaboListe (med egne kantobjekter)

- **naboliste**-datastruktur utvider kantlistestrukturen med container over tilhørende kanter for hver node.



- Minnebruk $O(n + m)$.

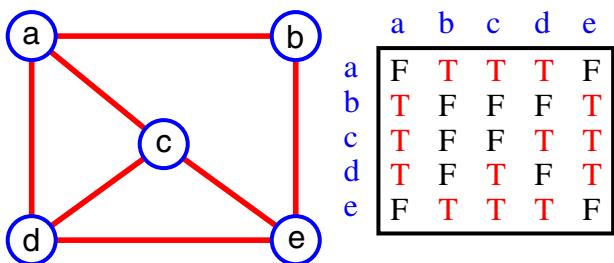
Kjøretid for NaboListe-Struktur

Operasjon	Tid
size, isEmpty, replaceElement, swap	$O(1)$
numVertices, numEdges	$O(1)$
vertices	$O(n)$
edges, directedEdges, undirectedEdges	$O(m)$
elements, positions	$O(n+m)$
endVertices, opposite, origin, destination, isDirected, degree, inDegree, outDegree	$O(1)$
incidentEdges(v), inIncidentEdges(v), outIncidentEdges(v), adjacentVertices(v), inAdjacentVertices(v), outAdjacentVertices(v)	$O(\deg(v))$
areAdjacent(u, v)	$O(\min(\deg(u), \deg(v)))$
insertVertex, insertEdge, insertDirectedEdge, removeEdge, makeUndirected, reverseDirection,	$O(1)$
removeVertex(v)	$O(\deg(v))$

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Nabomatrise (uten egne kantobjekter)



- matrise M for alle par av noder
- $M[i,j] = \text{True}$ om kant (i,j) finnes i grafen.
- $M[i,j] = \text{False}$ om det ikke er en kant (i,j) i grafen
- Minnebruk= $O(N^2)$.

NaboMatrise (med egne kantobjekter)

- Lagre selve kantobjektet i matrisen.

	0	1	2	3	4	5	6
0	\emptyset	\emptyset	$\text{NW } 35$	\emptyset	$\text{DL } 247$	\emptyset	\emptyset
1	\emptyset	\emptyset	\emptyset	$\text{AA } 49$	\emptyset	$\text{DL } 335$	\emptyset
2	\emptyset	$\text{AA } 1387$	\emptyset	\emptyset	$\text{AA } 903$	\emptyset	$\text{TW } 45$
3	\emptyset	\emptyset	\emptyset	\emptyset	\emptyset	$\text{UA } 120$	\emptyset
4	\emptyset	$\text{AA } 523$	\emptyset	\emptyset	$\text{AA } 411$	\emptyset	\emptyset
5	\emptyset	$\text{UA } 877$	\emptyset	\emptyset	\emptyset	\emptyset	\emptyset
6	\emptyset	\emptyset	\emptyset	\emptyset	\emptyset	\emptyset	\emptyset

BOS DFW JFK LAX MIA ORD SFO
0 1 2 3 4 5 6

- Minnebruk $O(n^2 + m)$

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Kjøretid for nabomatrise-strukturen

Operasjon	Tid
size, isEmpty, replaceElement, swap	$O(1)$
numVertices, numEdges	$O(1)$
vertices	$O(n)$
edges, directedEdges, undirectedEdges	$O(m)$
elements, positions	$O(n+m)$
endVertices, opposite, origin, destination, isDirected, degree, inDegree, outDegree	$O(1)$
incidentEdges, inIncidentEdges, outIncidentEdges, adjacentVertices, inAdjacentVertices, outAdjacentVertices,	$O(n)$
areAdjacent	$O(1)$
insertEdge, insertDirectedEdge, removeEdge, makeUndirected, reverseDirection, setDirectionFrom, setDirectionTo	$O(1)$
insertVertex, removeVertex	$O(n^2)$